

# Influence of latest orbit reprocessing on multi-mission altimetry



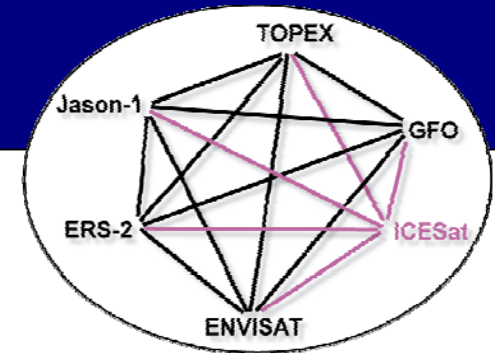
**Denise Dettmering & Wolfgang Bosch**

Deutsches Geodätisches Forschungsinstitut (DGFI)  
Centrum für Geodätische Erdsystemforschung (CGE)  
Munich, Germany  
email: *dettmering@dgfi.badw.de*

# Outline

- **Multi-Mission Crossover Analysis**
- **Orbit solutions**
  - **ESOC EIGEN-6C solutions (Jason-1/2, Envisat)**
  - **REAPER Orbits (ERS-1/2)**
  - **GFO GSFC std0905**
- **Investigations**
  - **Geographically correlated errors**
  - **Center-of-Origin (first degree harmonics)**
  - **Orientation of the rotation axis (second degree harmonics)**
- **Conclusion**

# Multi-Mission Cross-Calibration (MMXO)



## Basics

- single- and dual satellite crossover differences in all combinations
- using only crossovers close in time ( $\Delta t < 2$  days)
- least squares adjustment of radial errors minimizing crossover and the along-track consecutive differences
- Weighting of missions done by variance component estimation (VCE)
- TOPEX (later Jason1) taken as reference mission
- Segmentation into 10-day cycles of reference mission plus 2 days overlap (errors in the overlap differ by mm only)
- up to 120000(240000) crossovers (unknowns) per segment
- iterative solution with conjugate gradient algorithm

## Results

- time series of radial errors per mission (w.r.t. to reference mission)
- range bias (per 10 days period) => *Cal/Val Session*
- geographically correlated error pattern
- differences in the realization of the origin of reference frame (first order harmonics)
- differences in the realization of the rotation axis (second order harmonics)

*mainly due to orbit errors*

# Used orbit solutions

## ESOC sol3 & sol8 orbits (Jason-1/2 & Envisat)

- EIGEN-6C (including GOCE)
- ITRF2008

*Michiel Otten; ftp://dgn6.esoc.esa.int*

## ERS-1/2 REAPER Orbits

- ESA project “Reprocessing of Altimeter Products for ERS” (REAPER)
- Combined solution from three processing centers (DEOS,ESOC,GFZ)
- EIGEN-GL04S
- LPOD2005

*S. Rudenko, M. Otten, P. Visser, R. Scharroo, T. Schoene*

*New improved homogeneous orbits of ERS-1 and ERS-2 satellites, Advances in Space Research, submitted*

## GFO GSFC std09/05 Orbits

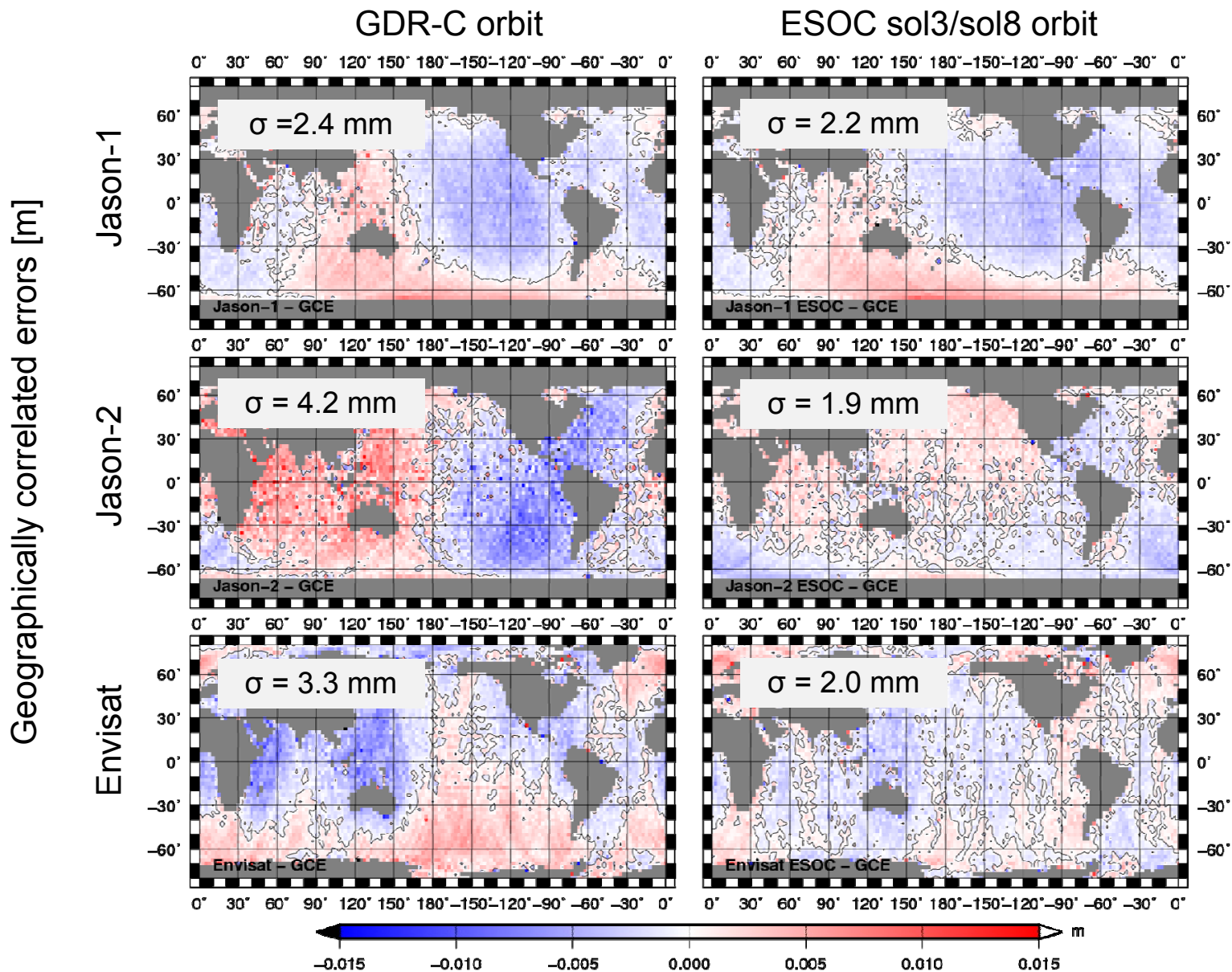
- EIGEN-GL04S (120)
- ITRF2005

*Lemoine F.G., Zelensky N.P., Chinn D.S., Beckley B.D., Lillibridge J.L.*

*Towards the GEOSAT Follow-On Precise Orbit Determination Goals of High Accuracy and Near-Real-Time Processing, Proceedings of AIAA/AAS Astrodynamics Specialist Conference 2006*

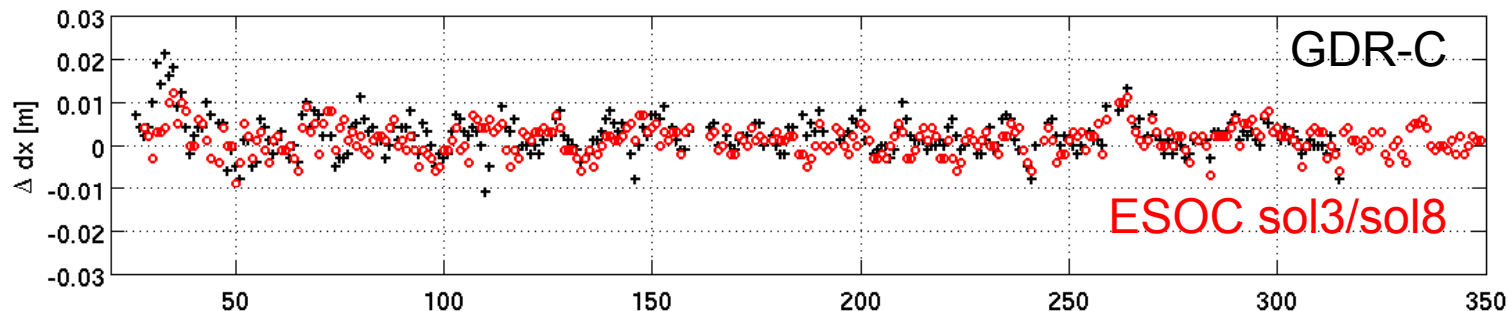
# ESOC EIGEN-6C orbits

# ESOC EIGEN-6C orbits – GCE

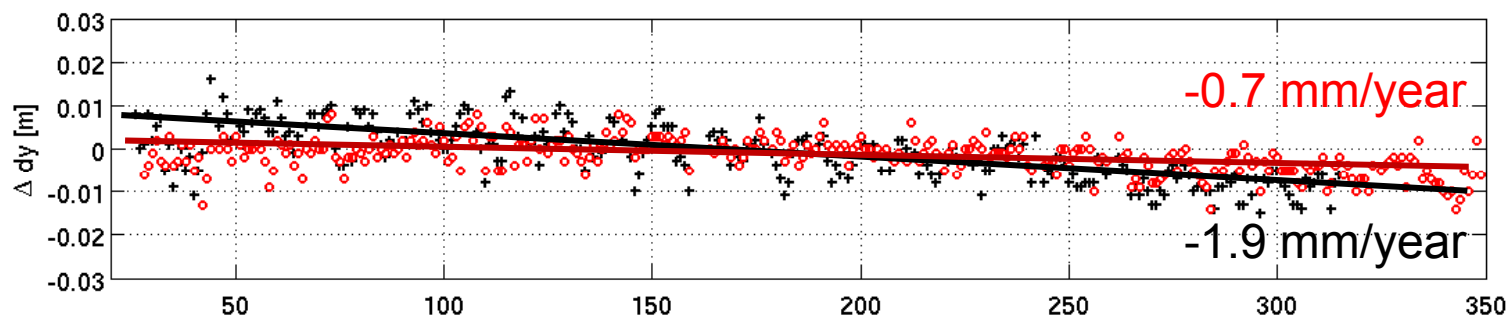


# ESOC EIGEN-6C orbits – Center of origin

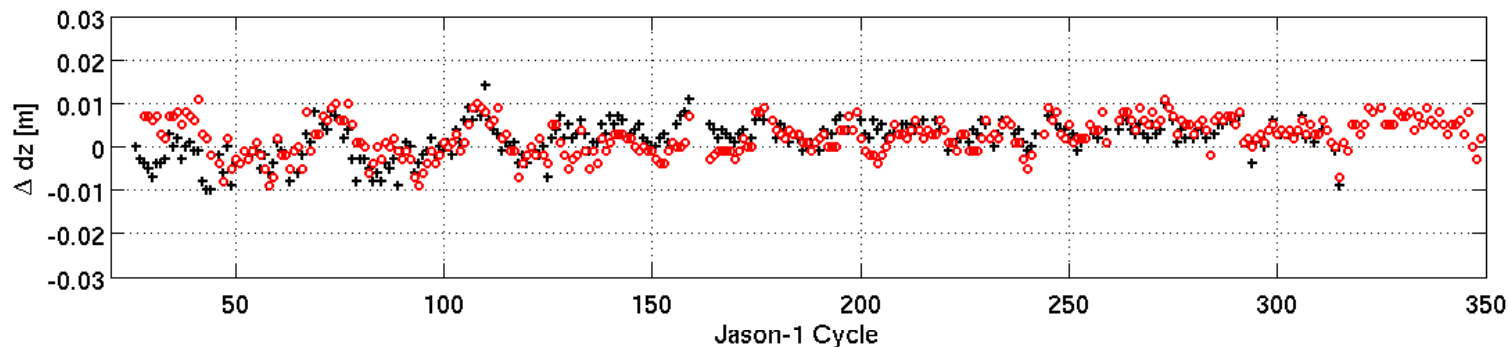
Relative differences in center-of-origin realization: Envisat-Jason1



$2.2 \pm 4.2$  mm  
 $1.2 \pm 3.4$  mm



$-1.0 \pm 6.3$  mm  
 $-1.6 \pm 4.0$  mm

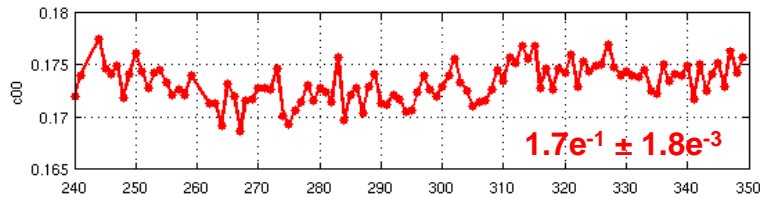


$1.8 \pm 4.0$  mm  
 $2.3 \pm 4.0$  mm

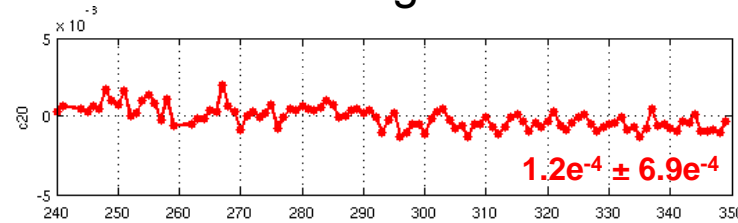
# Jason-2 – Low degree harmonics (ESOC sol3 orbit)

$$radial\ errors(\theta, \lambda) = \sum_{n=0}^2 \sum_{m=0}^n \left[ \bar{c}_{nm} \bar{P}_{nm}(\cos \theta) \cos m\lambda + \bar{s}_{nm} \bar{P}_{nm}(\cos \theta) \sin m\lambda \right]$$

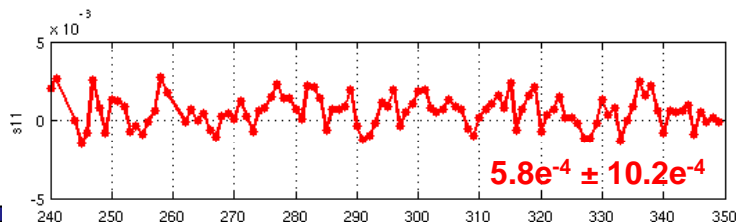
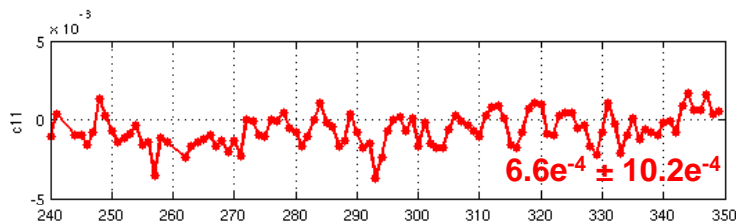
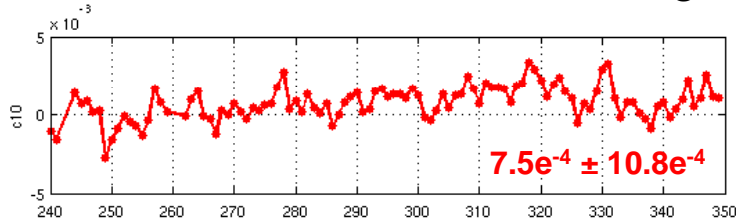
c00 => range bias



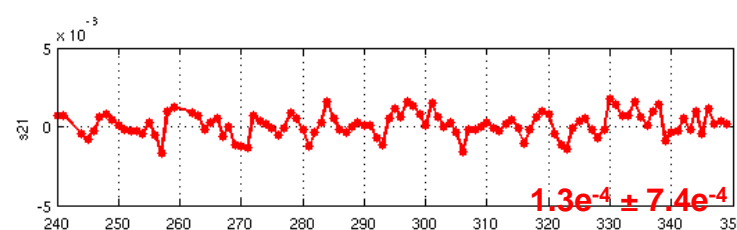
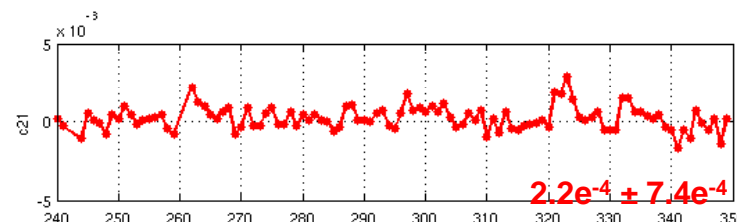
c20 => flattening



c10, c11, s11 => center-of-origin



c21, s21 => orientation of the rotation axis

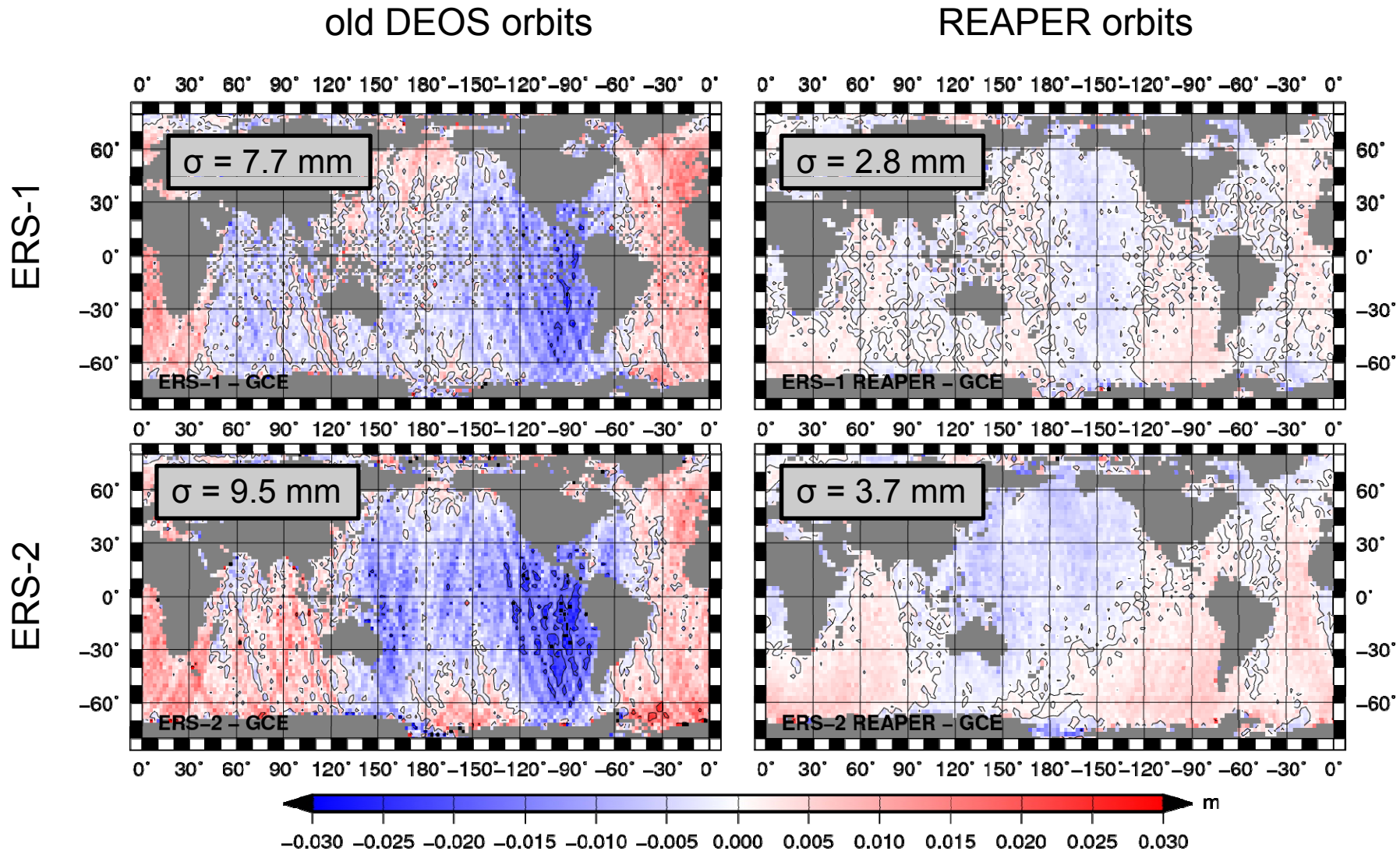


=> significant range bias w.r.t. Jason-1  
=> all other coefficients not significant

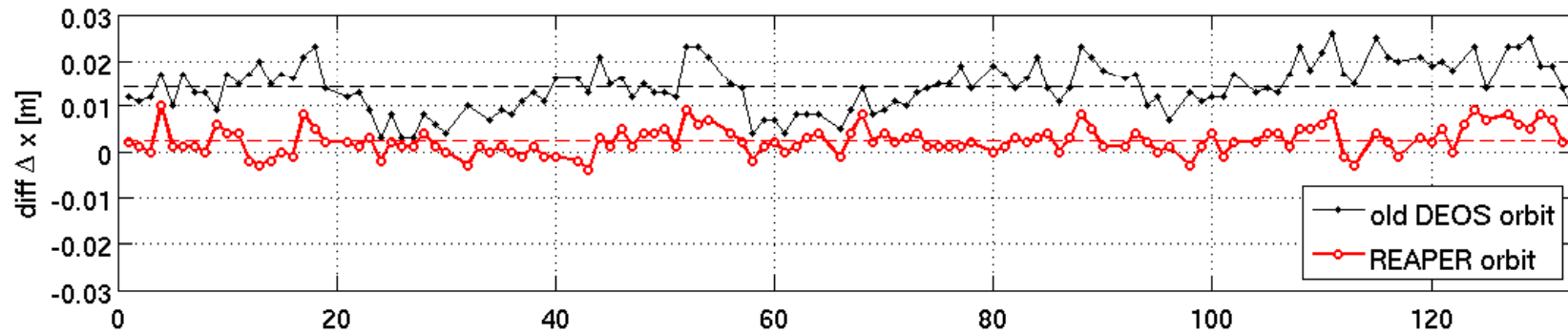


# ERS REAPER orbits

# ERS – geographically correlated errors

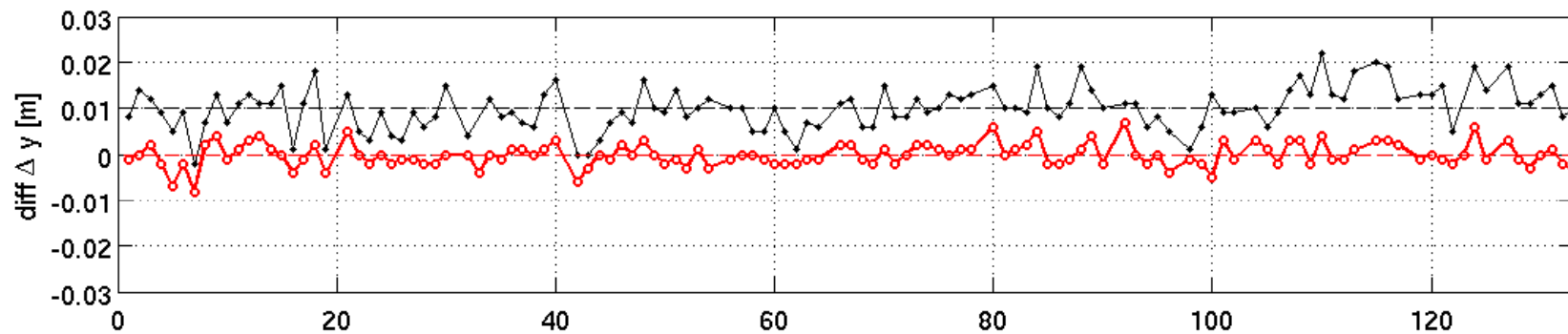


# Differences in Center-of-Origin realization: ERS1-TOPEX



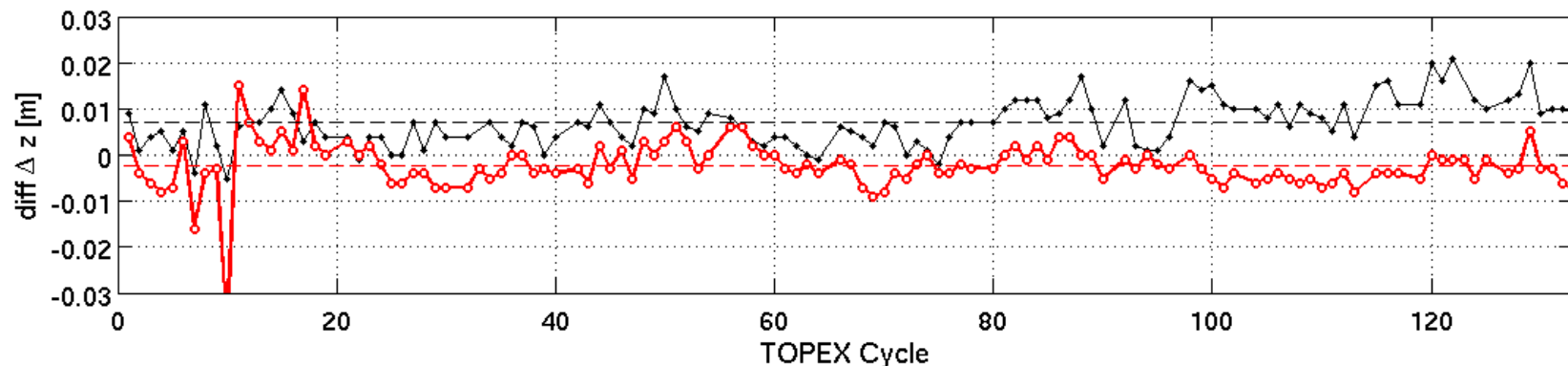
$14.2 \pm 5.4$  mm

$2.3 \pm 2.9$  mm



$10.0 \pm 4.7$  mm

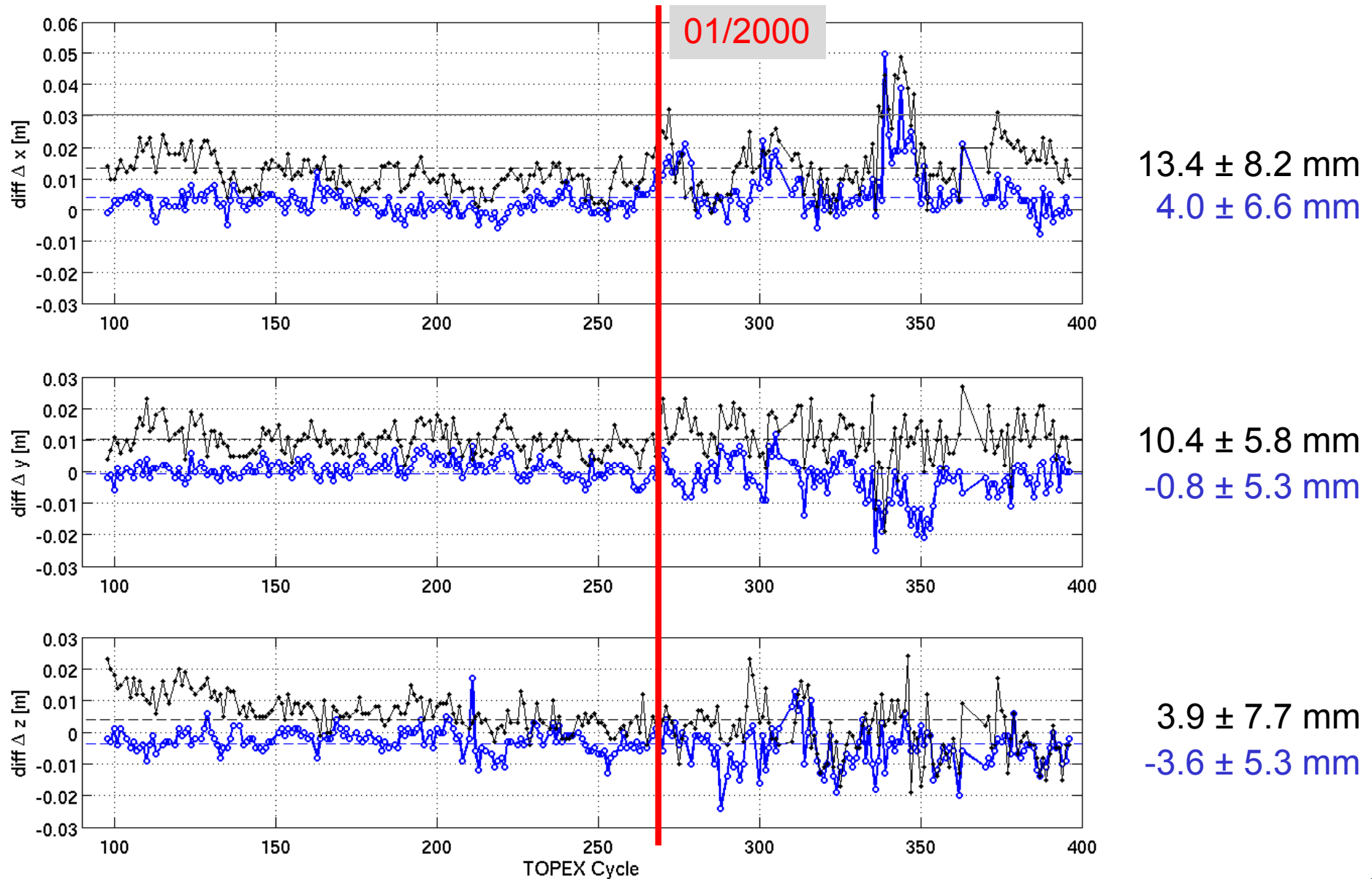
$-0.1 \pm 2.5$  mm



$7.0 \pm 5.1$  mm

$-2.3 \pm 5.5$  mm

# Differences in Center-of-Origin realization: ERS2-TOPEX



# ERS – center of origin

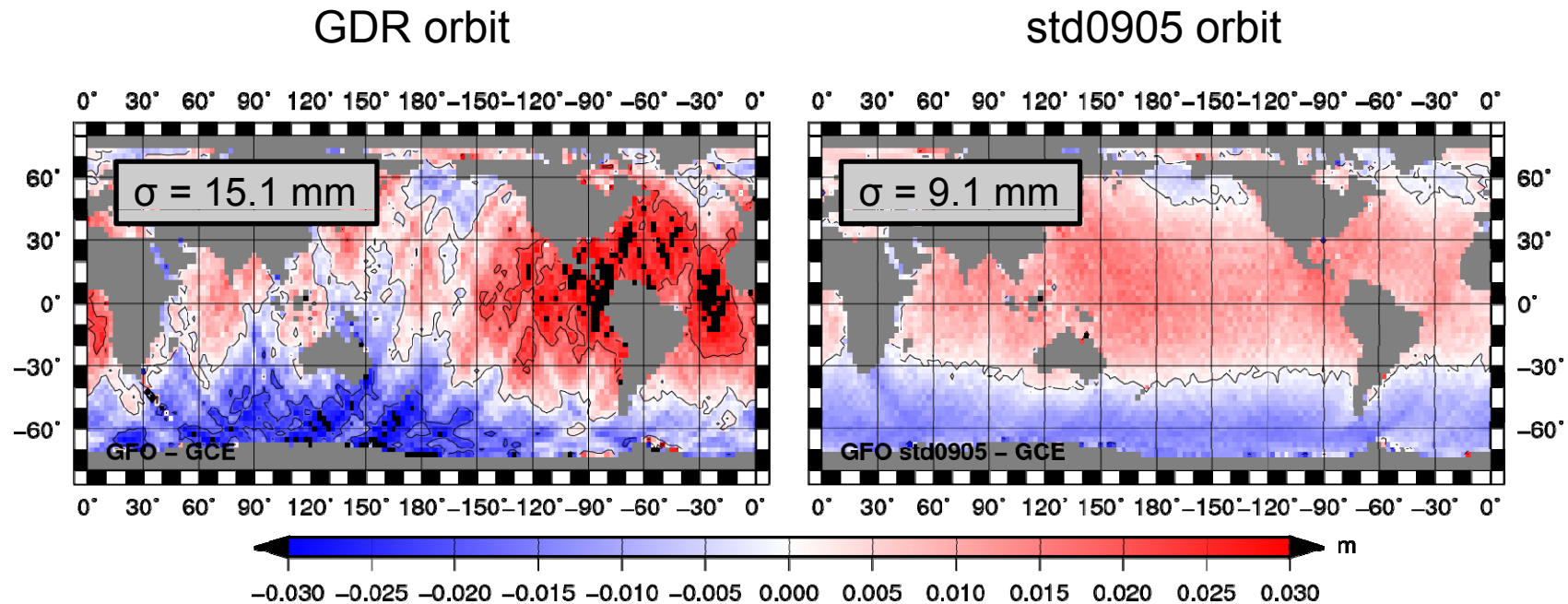
	ERS-1	ERS-2
dx	$2.3 \pm 2.9$	$4.0 \pm 6.6$
dy	$-0.1 \pm 2.5$	$-0.8 \pm 5.3$
dz	$-2.3 \pm 5.5$	$-3.6 \pm 5.3$

differences to TOPEX in [mm]

- ⇒ No significant differences in the center-of-origin realization between ERS REAPER orbits and TOPEX
- ⇒ ERS-2 higher variations due to increased solar activity (~2000 to 2003)
- ⇒ no significant differences in the second order terms (rotation axis)

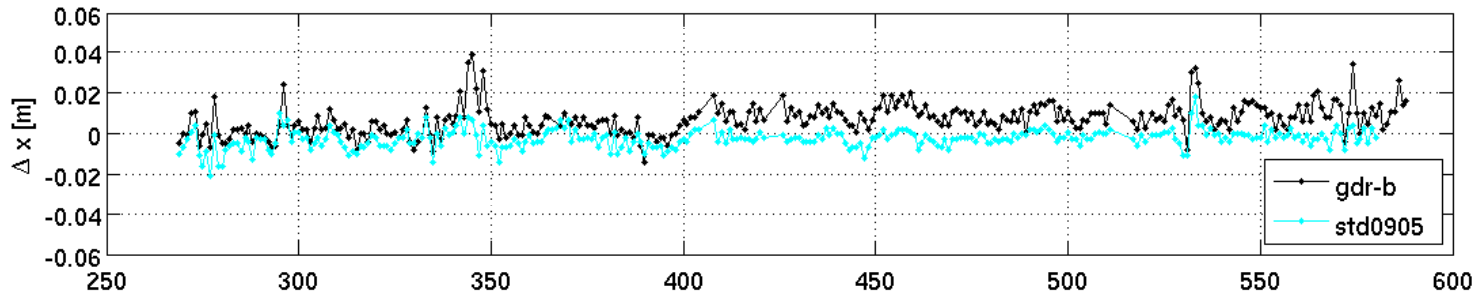
# GFO GSFC std0905

# GFO – geographically correlated errors

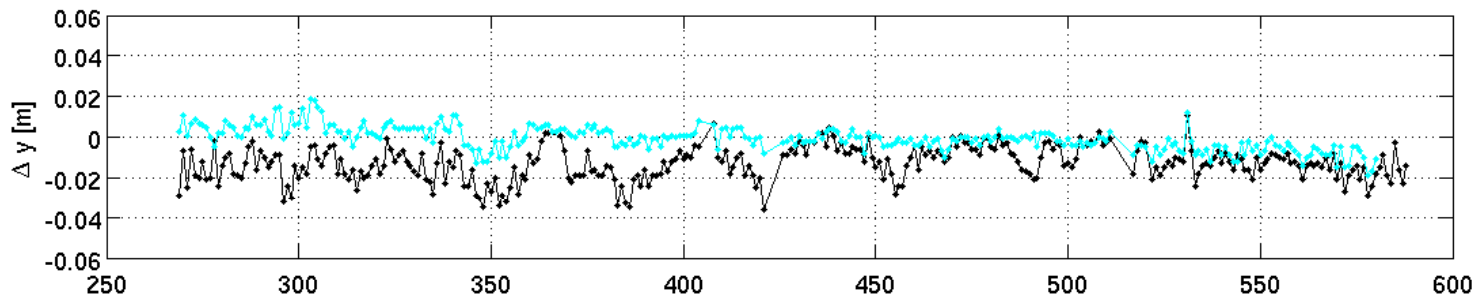


- ⇒ significant improvement
- ⇒ still some systematic effects left => J2 ?

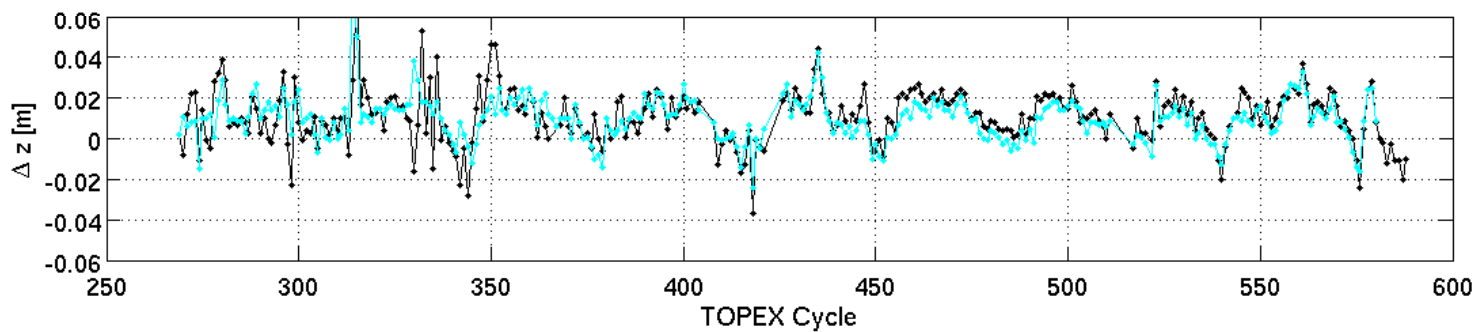
# GFO – center of origin



$7.0 \pm 7.5$  mm  
 $-2.6 \pm 4.6$  mm



$-0.6 \pm 6.0$  mm  
 $-13.0 \pm 8.3$  mm



$10.8 \pm 13.3$  mm  
 $9.9 \pm 10.8$  mm



# GFO – Low degree harmonics (w.r.t TOPEX mission)

	<b>gdr-b</b>	<b>std0905</b>
$C_{00}$	$21.6 \pm 5.3$	$23.9 \pm 4.5$
$C_{10}$	$5.7 \pm 7.5$	$5.2 \pm 6.2$
$C_{11}$	$4.3 \pm 3.9$	$-0.9 \pm 2.4$
$S_{11}$	$-6.5 \pm 4.4$	$0.8 \pm 2.9$
$C_{20}$	$-8.6 \pm 2.6$	$-6.4 \pm 2.1$
$C_{21}$	$-0.8 \pm 1.4$	$0.2 \pm 1.1$
$S_{21}$	$1.4 \pm 2.1$	$0.7 \pm 1.4$

range bias

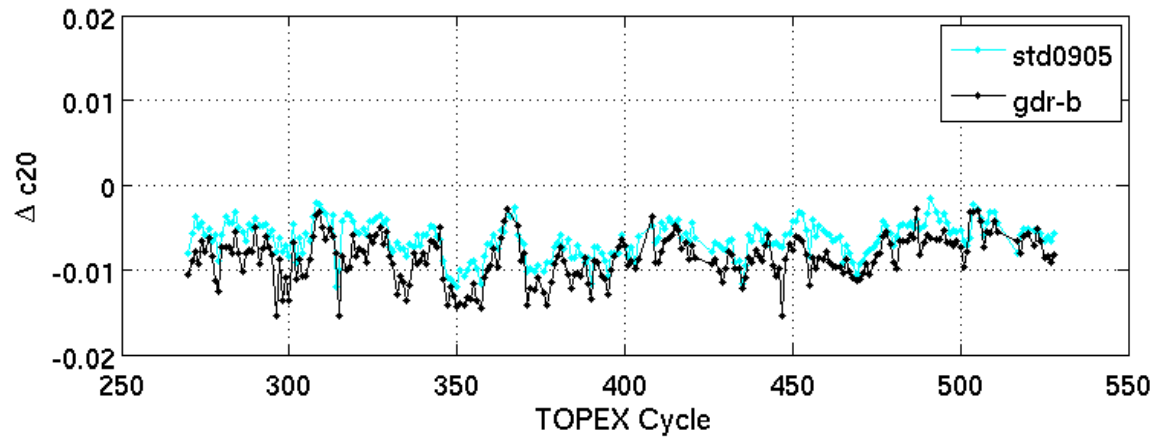
center-of-origin

flattening 

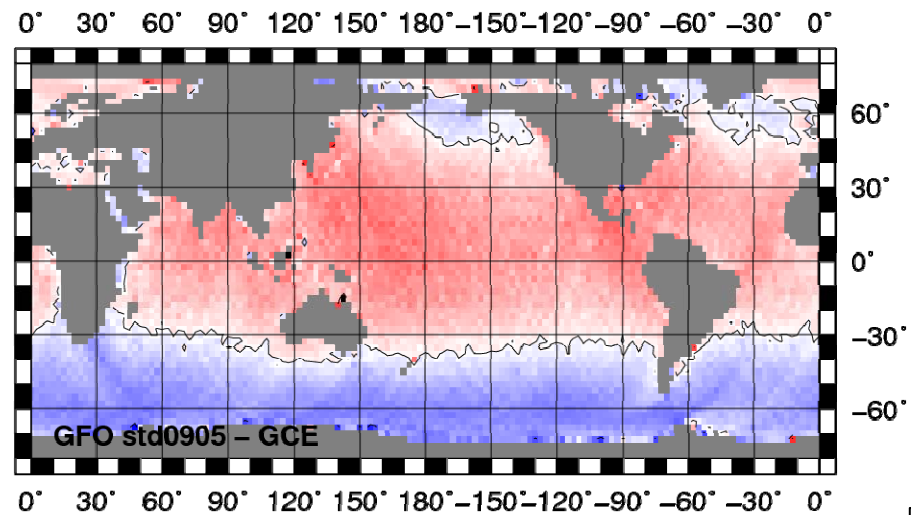
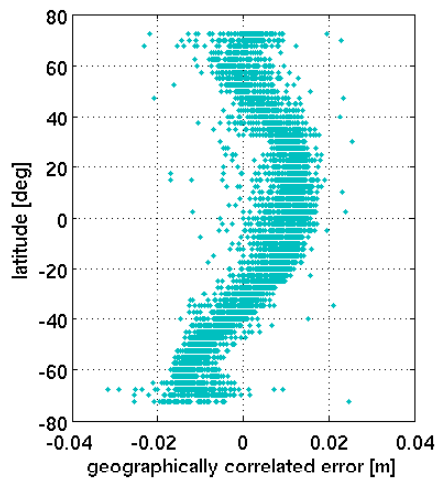
orientation of the rotation axis

- ⇒ center-of-origin differences reduced by std0905 orbit
- ⇒ significant difference in  $c_{20}$  (oblateness of the Earth) w.r.t. TOPEX remains

# GFO – flattening c20



geographically correlated errors



# Conclusion

- ✓ ESOC EIGEN-6C orbits: improved GCE and better consistency between **Jason** and **Envisat** (temporal gravity field, visible as  $\Delta y$ )
- ✓ Geographically correlated errors of **ERS** now in the same order of magnitude as TOPEX and Jason (2-3 mm RMS), thanks to REAPER!
- ✓ **GFO** orbits show significant improvement; some problems left: J2 systematic? Time tag bias?

THANK YOU !

# Computation of geographical correlated errors

Radial Errors are available for ascending and descending tracks.

From the differences between ascending and descending errors (mean values per 2.5° by 2.5° region) the mean GCE can be computed:

$$\Delta\gamma = (dr^{asc} + dr^{desc}) / 2 \quad [\text{Rosborough, 1986}]$$

- $dr^{asc}$  average of the radial errors (mean reduced) of all asc. passes
- $dr^{desc}$  average of the radial errors (mean reduced) of all desc. passes
- $\Delta\gamma$  mean of ascending and descending errors, GCE per cell

# Center-of-Origin Shifts

Separation of radial errors into range bias and center-of-origin shifts

Least square adjustment for each 10-day cycle

$$x_i + \varepsilon_{x_i} = \Delta r + \Delta x \cos \varphi_i \cos \lambda_i + \Delta y \cos \varphi_i \sin \lambda_i + \Delta z \sin \varphi_i$$

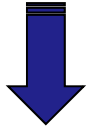
input: radial errors  $x_i$  at location  $\varphi_i, \lambda_i$

output: mean range bias  $\Delta r$

mean center-of-origin shifts  $\Delta x, \Delta y, \Delta z$

# Computation of low degree harmonics

radial errors



$$f(\theta, \lambda) = \sum_{n=0}^2 \sum_{m=0}^n \left[ \bar{c}_{nm} \bar{P}_{nm}(\cos \theta) \cos m\lambda + \bar{s}_{nm} \bar{P}_{nm}(\cos \theta) \sin m\lambda \right]$$



$\bar{c}_{00}$	range bias	$\bar{c}_{20}$	flattening
$\bar{c}_{10}$	center-of-origin z	$\bar{c}_{21}$	rotation axis
$\bar{c}_{11}$	x	$\bar{s}_{21}$	
$\bar{s}_{11}$	y		

$\bar{s}_{22}$   $\bar{c}_{22}$  : for most missions estimation not possible