



# **Comparison of Retrieval Algorithms for the Wet Tropospheric Path Delay**

# Introduction

## Objective :

- Theoretical evaluation of current regression algorithms for the retrieval of the wet tropospheric path delay (dh) :
  - How different are the operational algorithms ?
  - Can we improve those algorithms ?

## Outline :

- The wet tropospheric correction
- Algorithms currently used in altimetry missions
- Comparison of two algorithms: log-linear vs neural network
- Correlation analysis of inputs
- Conclusion

# The wet tropospheric path delay

- Corresponds to path delay in the radar return signal due to water vapor in the troposphere
- Ranges from 0 to 50 cm.
- Any error in the wet-tropospheric correction directly impacts the sea level determination
- Calculated from radiometer measurements with uncertainty of around 1-cm rms (Ruf et al. 1994)

# The wet tropospheric path delay retrieval

- Microwave radiometers measure brightness temperature (natural emission of sea surface and atmosphere)
- $t_b$  measured at a given frequency depends on the atmospheric profile and on sea surface conditions
- 3  $t_b$ s usually used around :
  - $t_{b24GHz}$  : highly sensitive to water vapor ( $wv$ )
  - $t_{b37GHz}$  : sensitive to clouds ( $wc$ )
  - $t_{b18GHz}$  : sensitive to the surface : temperature ( $ts$ ) and roughness.
- Relationship between  $d_h$  and  $t_b$  is established through statistical regression

# Two families of retrieval algorithms



NASA/CNES/NOAA/Eumetsat:  
TOPEX/JASON1/JASON2

- RTM
- Radiosondes and Radiometers
- $tb_{18.7}$ ,  $tb_{23.8}$ ,  $tb_{34}$
- Two-step log-linear regression

Keihm et al. 1995



ESA (+CNES/ISRO ALTIKA):  
ERS1/ERS2/ENVISAT/SENTINEL3

- RTM
- ECMWF Fields
- $wspd/sigKu$ ,  $tb_{23.8}$ ,  $tb_{36.5}$
- Neural Network

Eymard et al. 1996/Obligis et al. 2006

# Comparison of 2 Algorithms

2012 ECMWF fields + UCL RTM :

20% for learning and 80% for testing

JMR\_Reg

Two-step log-linear  
regression

tb18.7 +tb23.8 +tb34

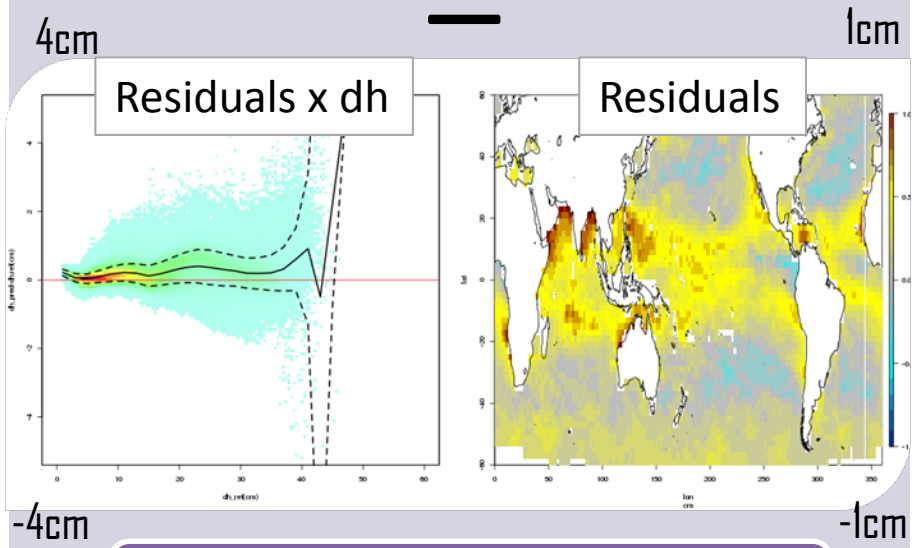
MWR\_NN

Neural Network

sigKu + tb23.8 + tb34

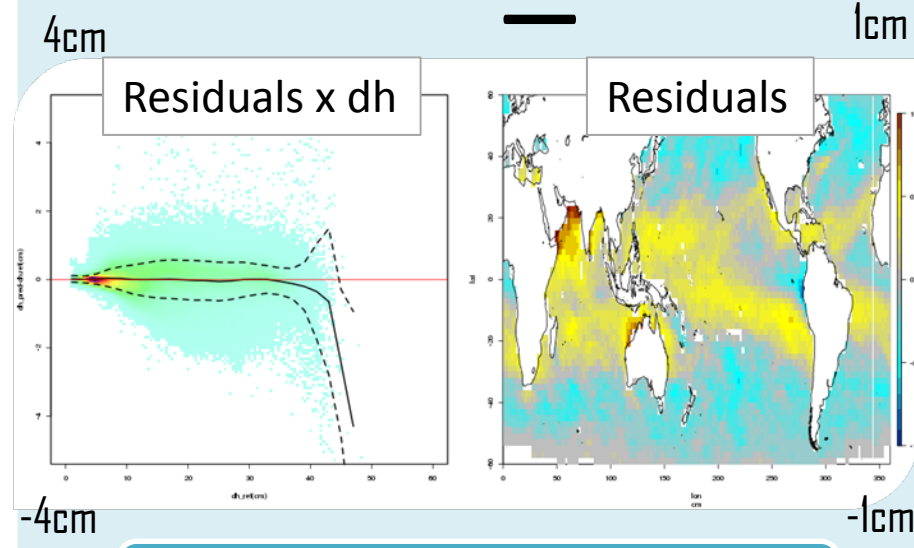
# Results on the test database

## JMR\_REG



RMS = 4.34 mm

## MWR\_NN



RMS = 4.45 mm

# A third Algorithm

2012 ECMWF fields + UCL RTM :

20% for learning and 80% for testing

JMR\_Reg

JMR\_NN

MWR\_NN

Two-step log-linear regression

Neural Network

Neural Network

tb18.7 + tb23.8  
+ tb34

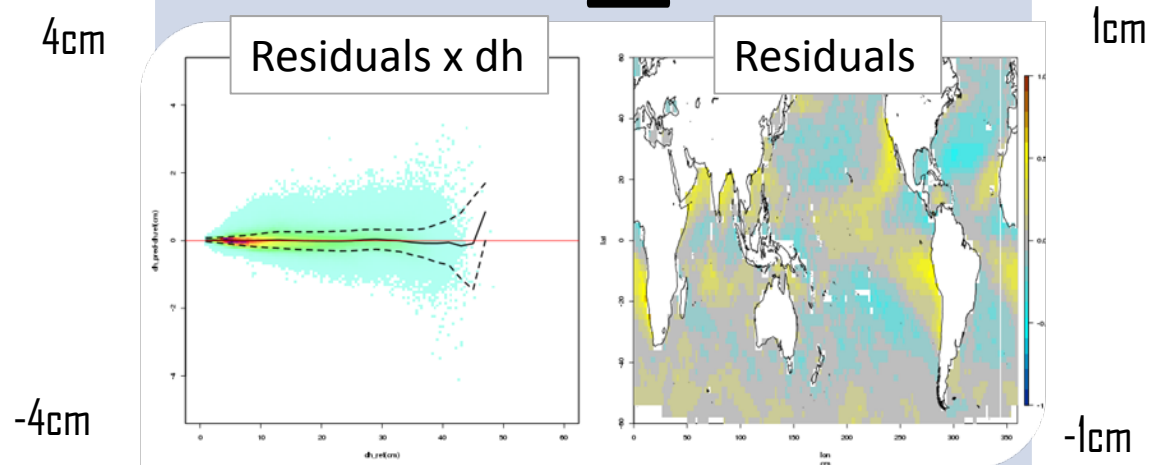
tb18.7 + tb23.8  
+ tb34

sigKu + tb23.8 +  
tb34



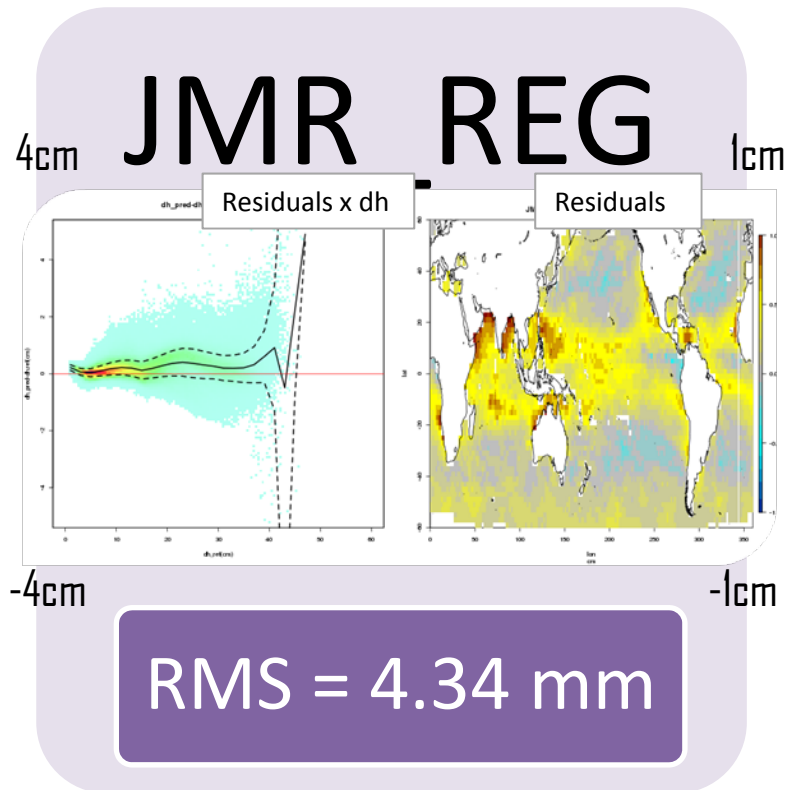
# Results on the test database

## JMR\_NN

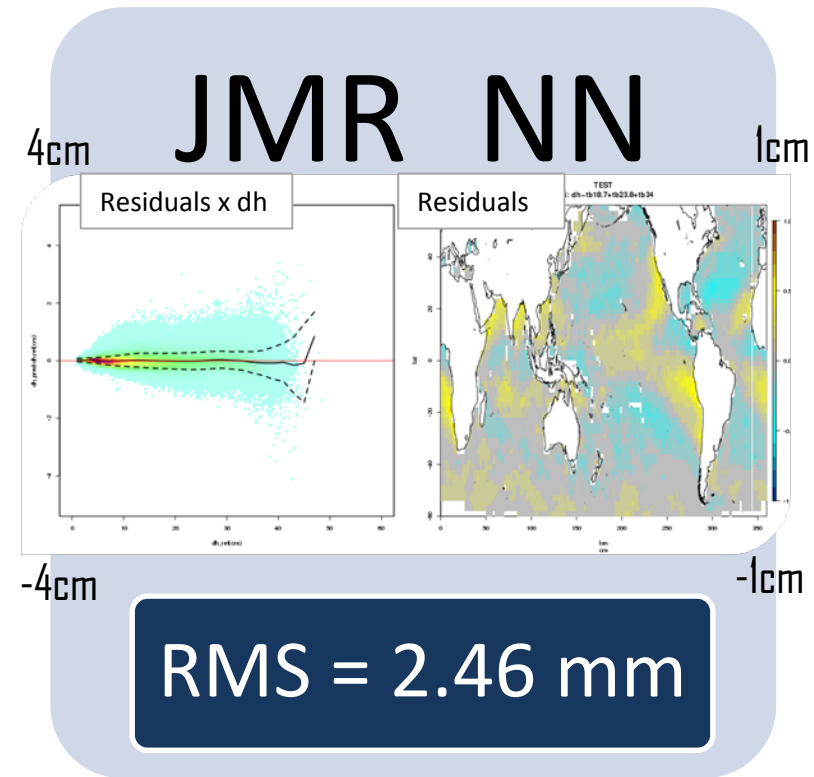


**RMS = 2.46 mm**

# Results on the test database



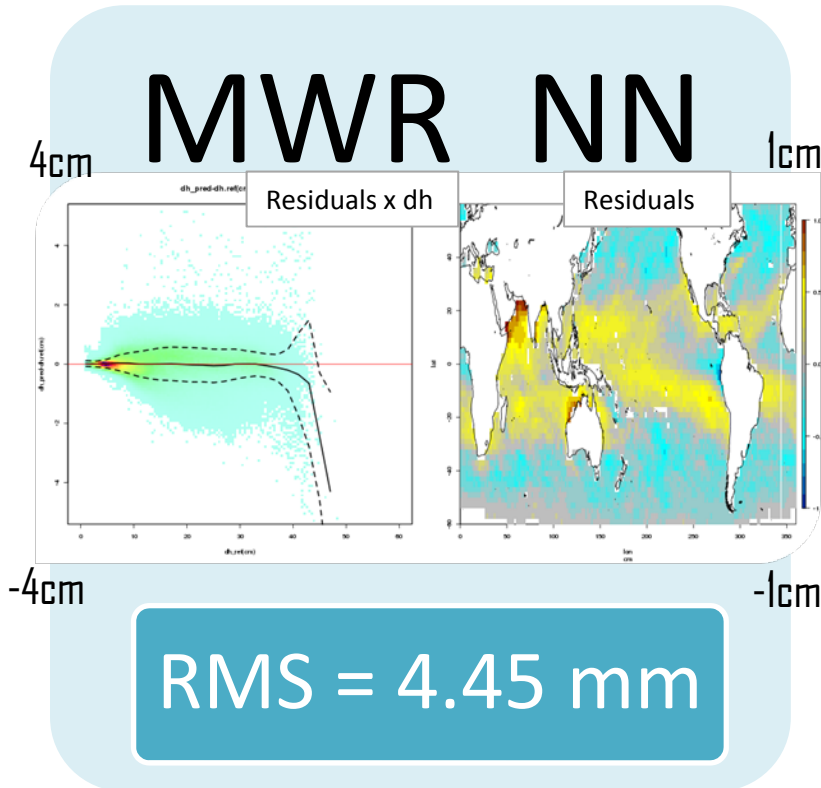
VS



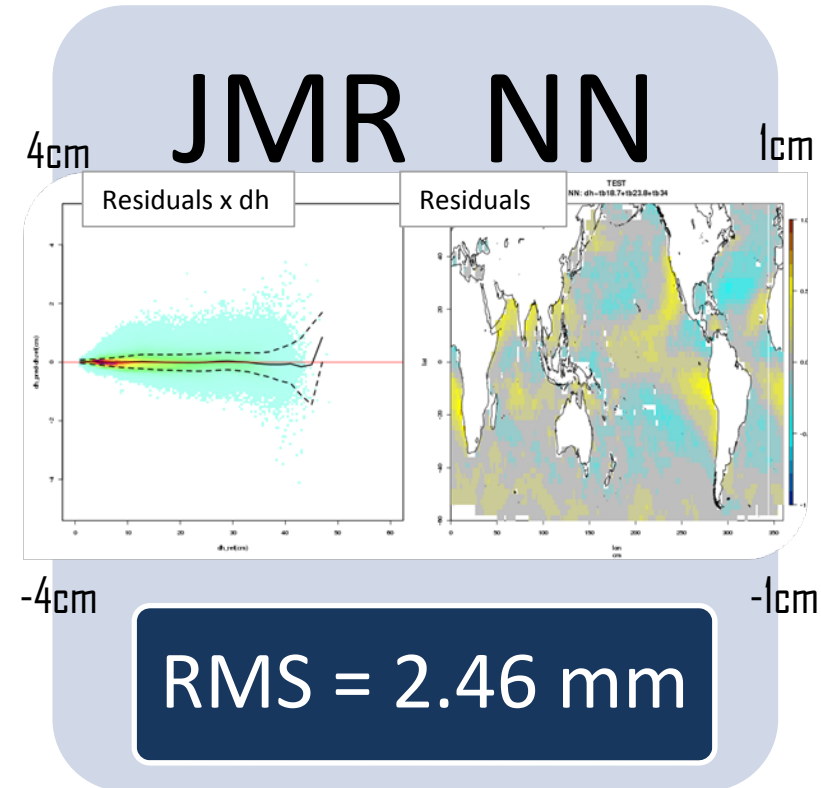
## TWO STEP LOG-LINEAR REGRESSION VS NEURAL NETWORK :

- dh-dependent bias for JMR\_REG
- The two step log-linear regression lacks flexibility to correctly adjust the data compared to neural networks

# Results on the test database



VS

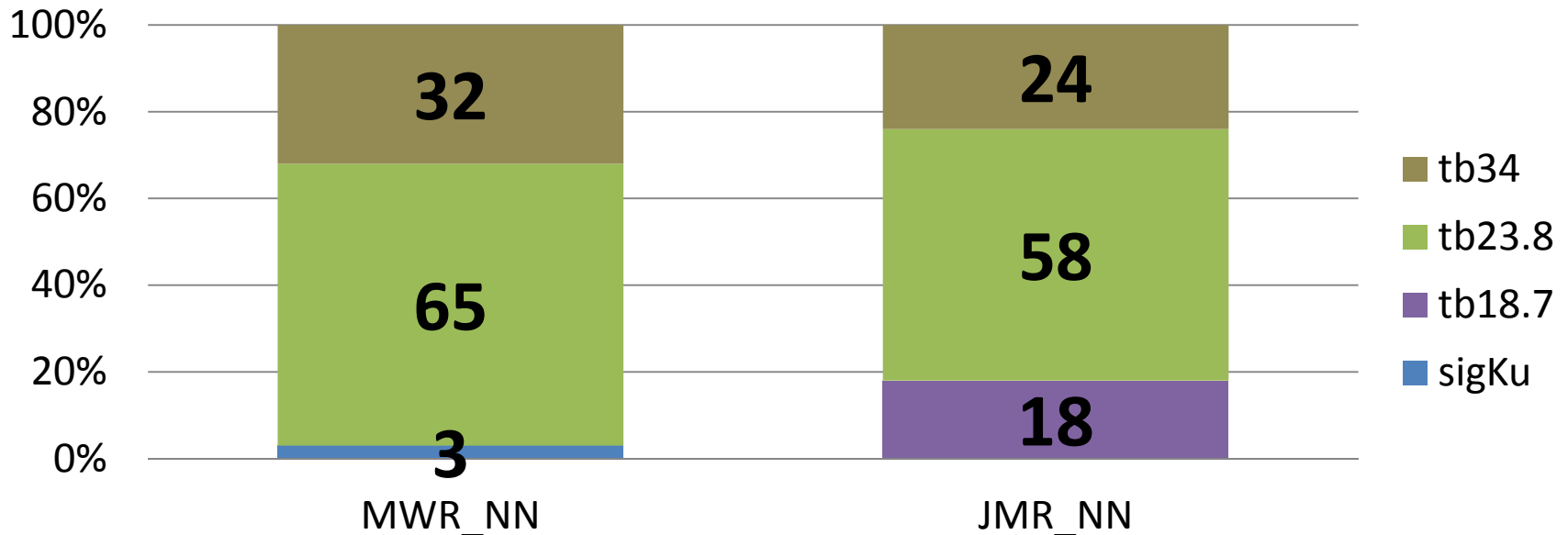


## SIGKU VS TB18.7:

- sigKu and tb18.7 do not bring equivalent information on the surface
- Use of tb18.7 gives much better performances

# Importance of inputs

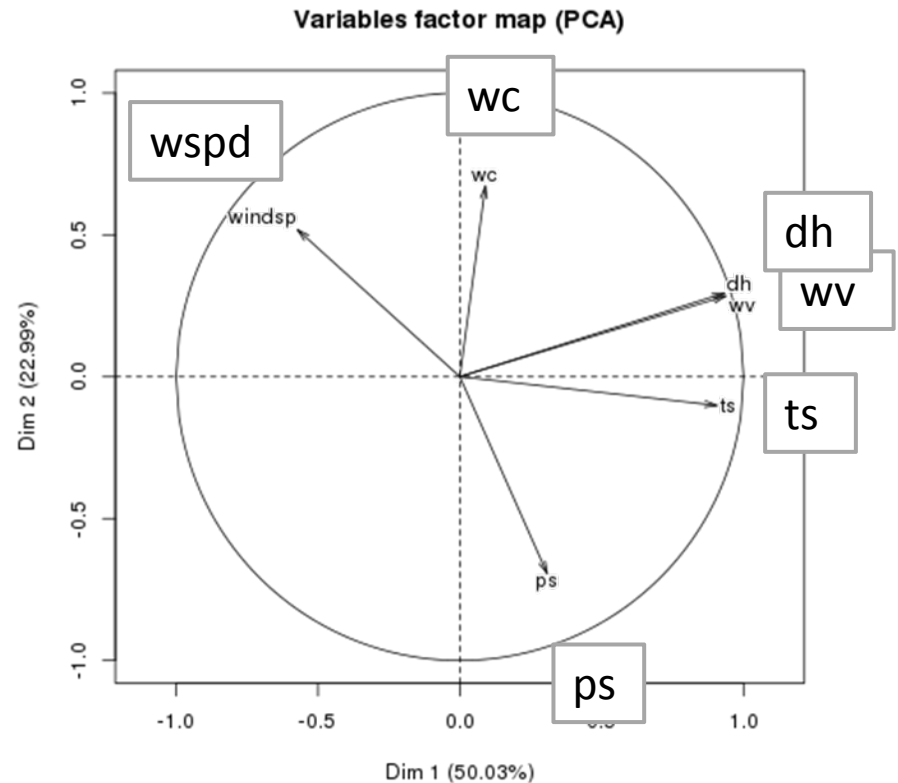
NN Input Relative Importance : HVS Criteria  
(YACOUB & BENNANI Y, 1997)



- sigKu is of little importance, compared to tb23.8 and tb34 for the retrieval of dh
- tb18.7 relative importance is much higher than sigKu relative importance

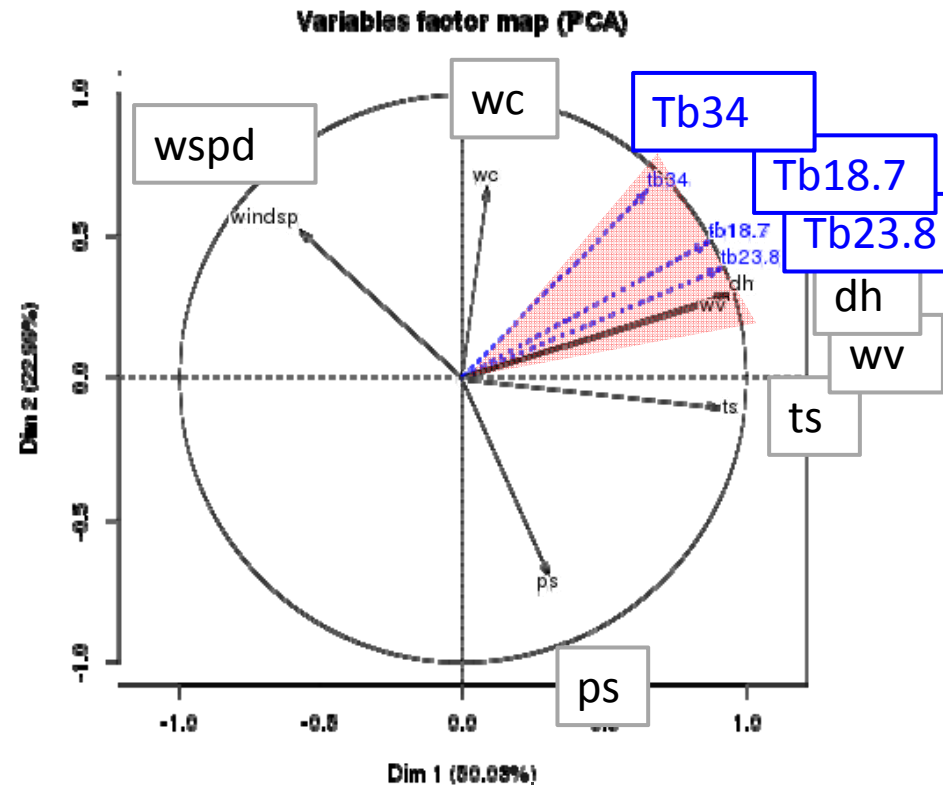
# Principal component analysis

- Applied to ts, windsp, wc, wv and dh.
- Best summary of correlation between variables
- Each variable is represented by a vector
- Correlation between two variables is given by cosines of the angle between the two vectors



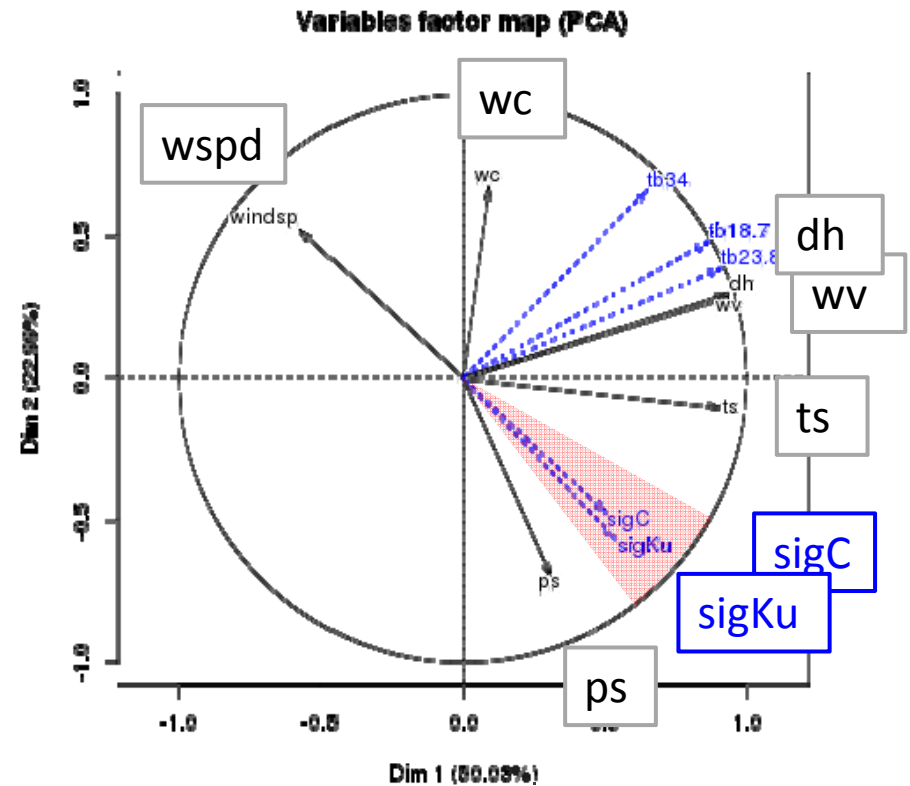
# PCA : Brightness Temperatures

- tb18.7, tb23.8 are highly correlated to dh and wv (*cor* > 0.90)
- tb23.8 is the most correlated to dh, wv and ts
- tb34 is the most affected by wc

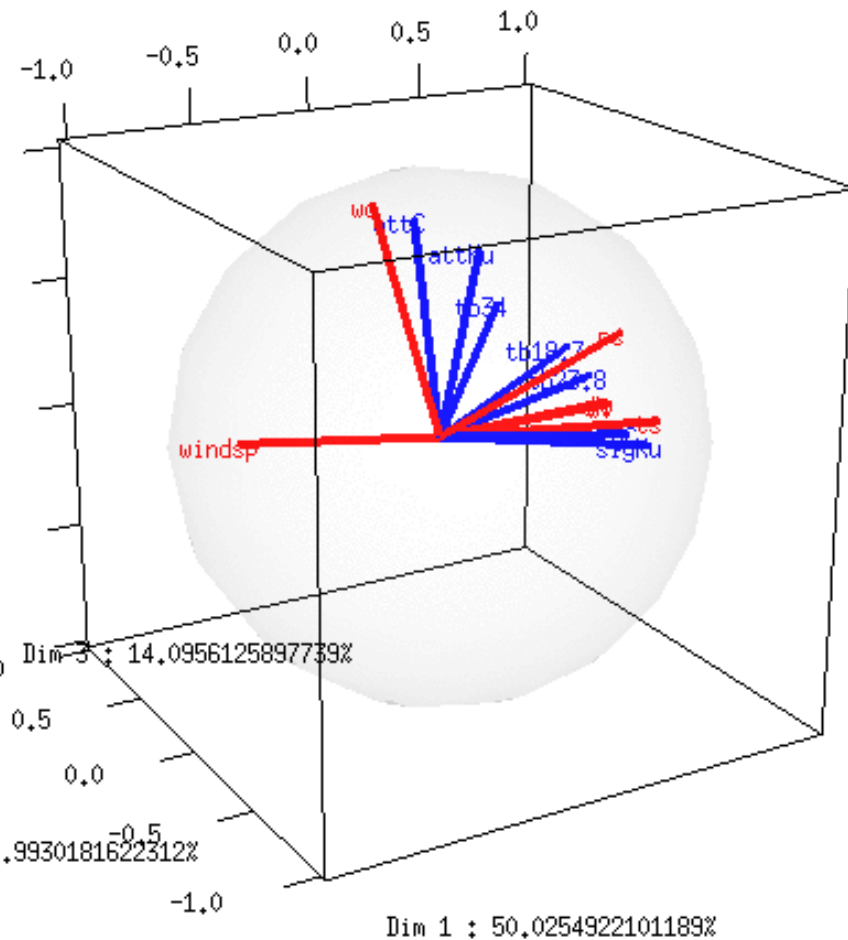


# PCA : Backscattering coefficients

- sigC and SiKu are highly correlated with windsp :  
 $cor(sigKu, windsp) = -0.99$ ,  
 $cor(sigC, windsp) = -0.93$
- Little correlations are found with dh, wv and tbs ( $cor < 0.30$ )



# PCA : Conclusions



- sigKu is closer to windsp and lacks information about ts and dh
- tb18.7 is closer to ts and dh
- MWR\_NN lacks information about ts ?



# Last Comparisons

MWR\_NN

- sigKu+tb23.8+tb37
- **RMS = 4.45 mm**

JMR\_NN

- tb18.7+tb23.8+tb37
- **RMS = 2.46 mm**

MWR\_NN+ts

- **ts**+sigKu+tb23.8+tb37
- **RMS = 2.21 mm**

# Conclusions

- Only an assessment of the regression quality on a given simulated database and not of the entire radiometric error budget (regression quality, database representativeness, RTM quality, instrumental noise, pixel heterogeneity, antenna pattern...)

## **BUT SUCH ANALYSIS HELPS :**

- Finding an appropriate method of regression :
  - **NN are more flexible than log-linear regressions.** NN are black-boxes but tools are being developed to make them more transparent.
- Identifying useful sources of information to improve the retrieval :
  - **sigKu** lacks correlation with dh and ts but **provide useful information on windsp** with respect to tb18.7
  - tb18.7 is more important than sigKu in the retrieval of dh : tb18.7 provides additional information on dh and ts => **3-channel radiometers should be preferred**
  - **Lack of 18.7 GHz channel can be compensated by ts for equivalent results.** Reynolds SST could probably be used for near real time dh products
- All these results should be assessed on real measurements using usual metrics (SSH variance at crossovers ,radiosonde comparisons...)