

# Can Geodetic-Mission Altimetry be used to Improve Maps of the Internal Tide?

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## Summary

Due to the large inter-track spacing of exact-repeat missions (ERM), direct estimates of the internal tide field are necessarily of coarse resolution, even when data from multiple exact-repeat altimeter missions are combined. Here, ERM, long-repeat (Cryosat2), and geodetic mission (GM) data are combined to map the tide at higher resolution. The proposed approach is likely to be useful only in special cases where the tide varies by 1 cm or more over length scales of 50 km.

## Spatial Density of Altimeter Data

At the latitude of Hawaii ERM pass density is approximately 280 passes per degree-squared; GM pass density is approximately 52 passes per degree-squared.

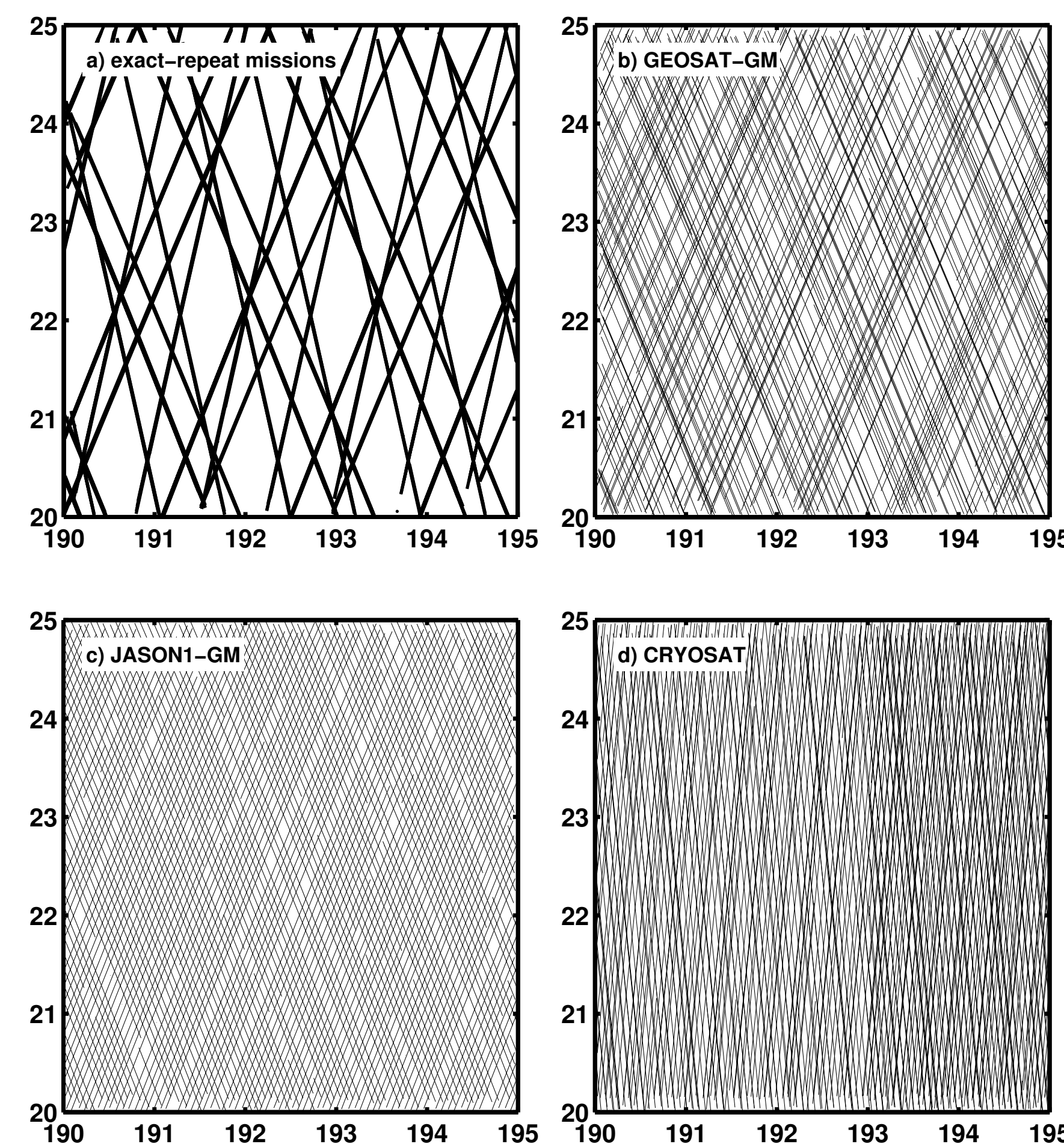


Table 1: ERM

| Name       | Start       | End         | # Repeats | Period |
|------------|-------------|-------------|-----------|--------|
| TOPEX-a    | 25 Sep 1992 | 11 Aug 2002 | 363       | 10     |
| TOPEX-b    | 20 Sep 2002 | 08 Oct 2005 | 112       | 10     |
| JASON1-a   | 15 Jan 2002 | 26 Jan 2009 | 258       | 10     |
| JASON1-b   | 10 Feb 2009 | 03 Mar 2012 | 112       | 10     |
| ERS2-a     | 29 Apr 1995 | 04 Jul 2011 | 169       | 35     |
| ENVISAT1-b | 14 May 2002 | 22 Oct 2010 | 88        | 35     |
| GFO1-a     | 07 Jan 2000 | 17 Sep 2008 | 192       | 17     |
| JASON2-a   | 04 Jul 2008 | 05 Sep 2013 | 190       | 10     |

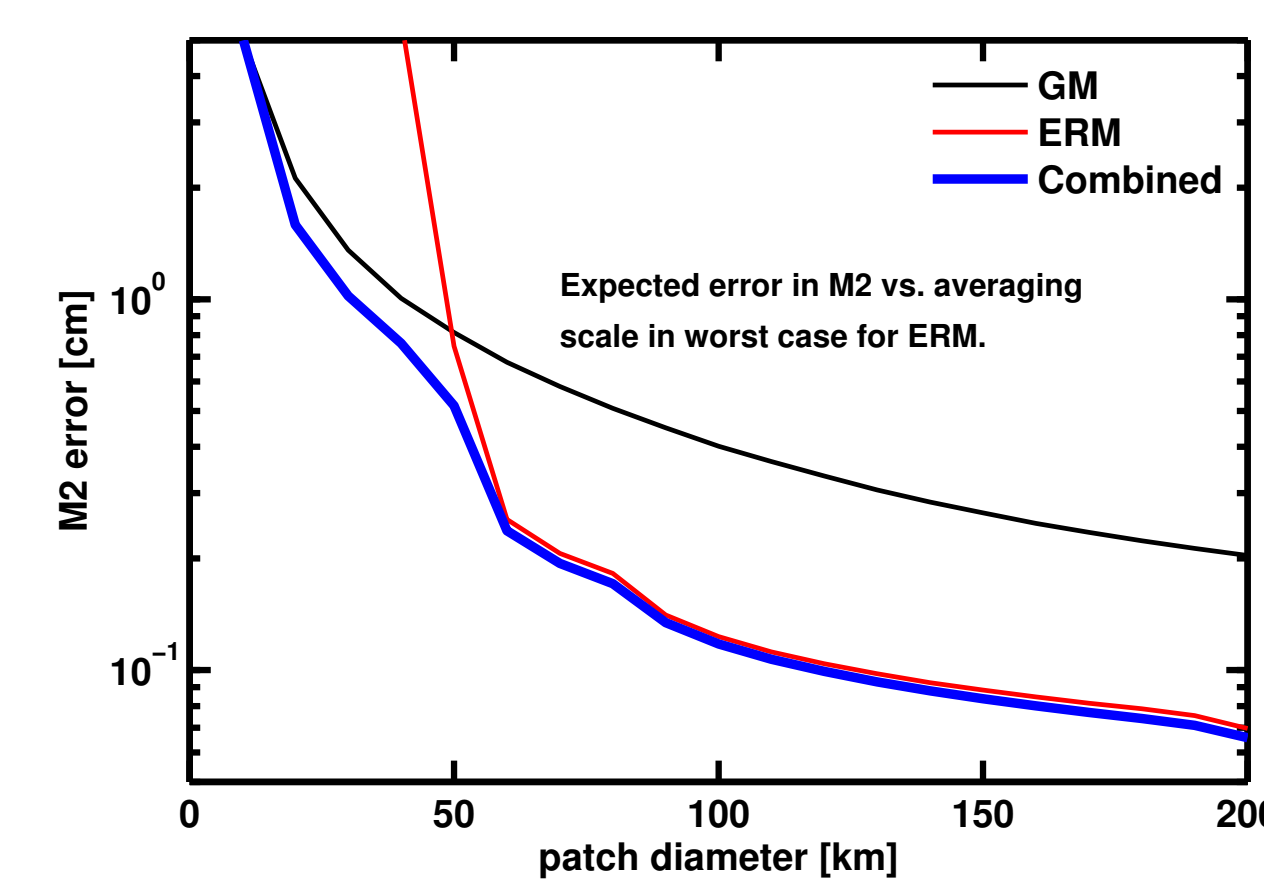
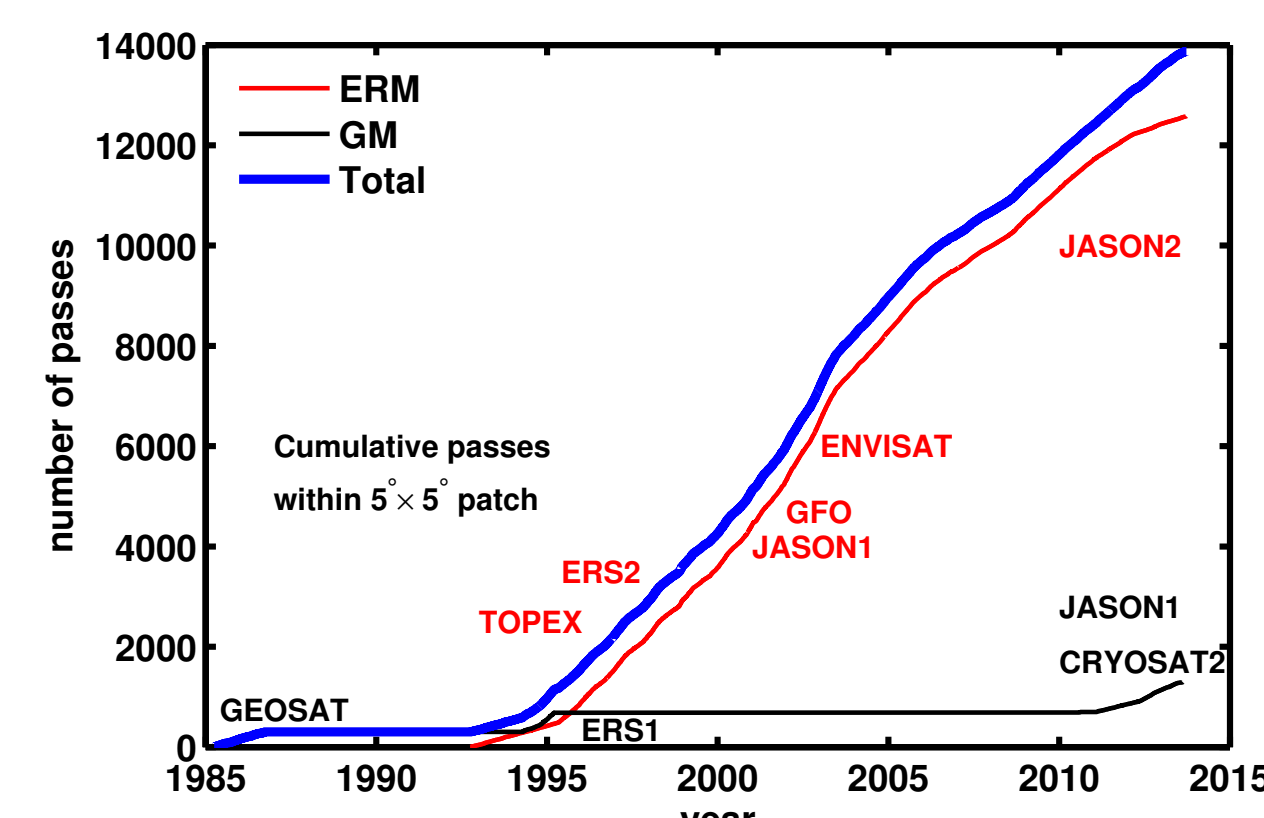
Table 2: GM and Cryosat2

| Name       | Start       | End         |
|------------|-------------|-------------|
| GEOSAT-a   | 31 Mar 1985 | 30 Sep 1986 |
| ERS1-e     | 10 Apr 1994 | 28 Sep 1994 |
| ERS1-f     | 28 Sep 1994 | 21 Mar 1995 |
| JASON1-c   | 07 May 2012 | 20 Jun 2013 |
| CRYOSAT2-a | 14 Jul 2010 | 06 Sep 2013 |

## Harmonic Analysis of Multi-Mission Data

Harmonic analysis with error estimates are computed using the standard least-squares methods. Nominal values of 3 cm for measurement noise and 15 cm for non-tidal SSH variability are assumed. Measurement precision of individual altimeters is not included. Precision of mean sea surface (and other corrections) along different ground tracks is not included.

- Uncertainty of tides from GM data are a factor of 3 to 4 worse than from combined ERM data when the averaging scale is greater than 70 km.
- GM data can be used to identify a 1 cm  $M_2$  tide at scales larger than 50 km.
- Alternately, GM data may be useful in resolving large amplitude (1 cm or more for  $M_2$ ) spatial variability in tidal fields at scales smaller than 50 km.
- Conclusion: GM data may contribute to tidal estimation only in special cases where there is sufficient tidal SSH variance at scales smaller than ERM ground track spacing.



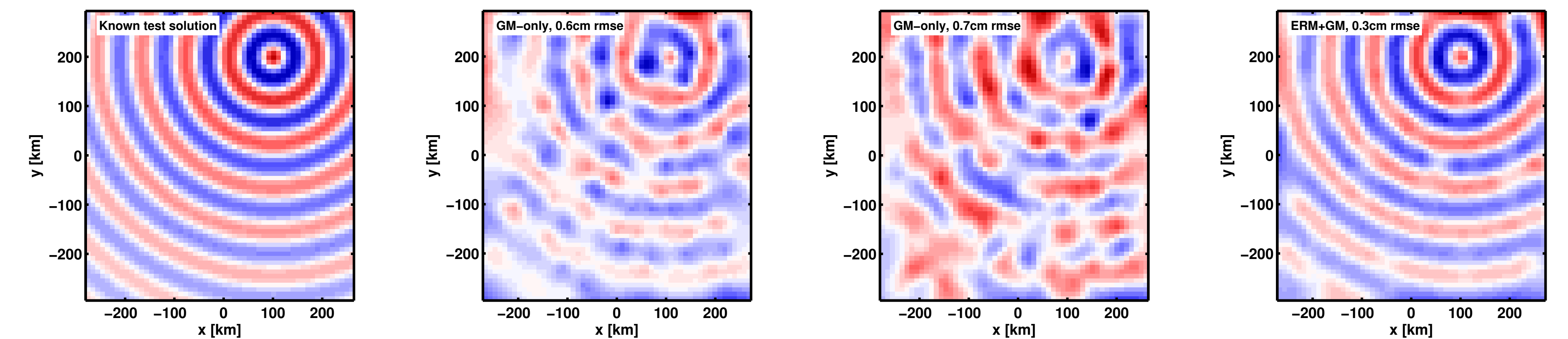
## Tidal Mapping via Spatially-Regularized Harmonic Analysis

Tides are mapped here by representing the SSH as a product of thin-plate splines in space and harmonic functions in time. The representation can be written as

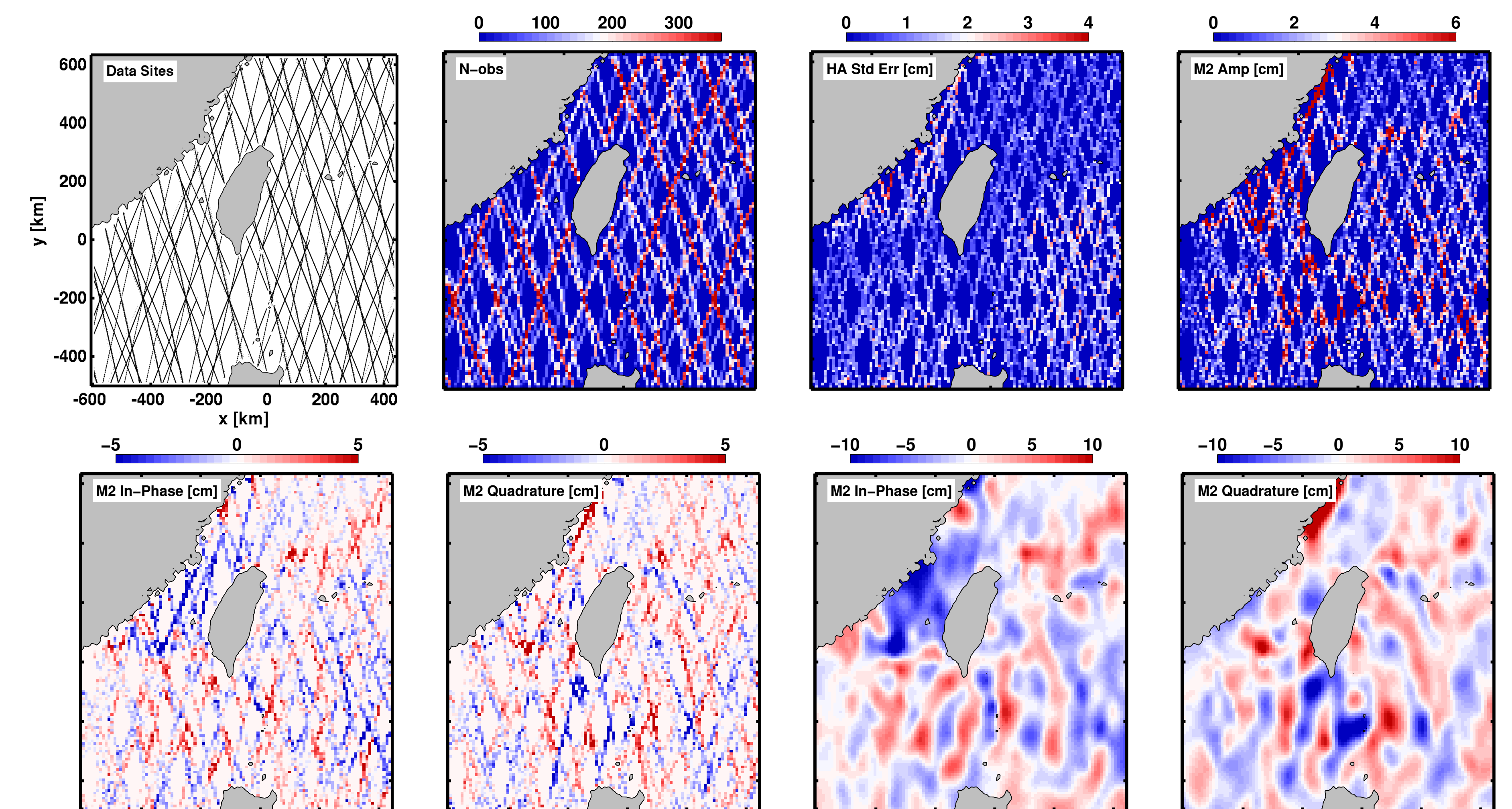
$$\hat{h}(\mathbf{x}, t) = \sum_{kl} \alpha_{kl} \phi_k(\mathbf{x}) \zeta_l(t) + \sum_{il} \beta_{il} \kappa(\mathbf{x} - \mathbf{x}_i) \zeta_l(t). \quad (1)$$

## Test Case: Reconstructing a 2.5 cm Mode-2 $M_2$ Signal in the Presence of 15 cm Non-Tidal Noise

In this test case a known solution is reconstructed from synthetic data based on ERM sampling, GM sampling, and their combination.



## Application: Mapping $M_2$ Near Taiwan and Luzon Strait



## Conclusions

- The problem of tidal estimation using Geodetic Mission (GM) altimetry has been analyzed and compared to approaches which use Exact Repeat Mission (ERM) data alone.
- A new approach to empirical mapping of tides has been implemented which combines harmonic analysis and thin-plate splines.
- GM altimetry will contribute to tidal estimation only in special cases where there is substantial coherent tidal SSH variance at scales smaller than ERM ground track spacing.
- NEXT STEPS: continue to validate the methodology; compute error estimates using estimate-based bootstrap; use physically-based basis functions instead of thin-plate splines.

## Acknowledgements

The altimeter data used here were extracted from the Radar Altimeter Database System (RADS).